

For **AQA**

# Mathematics

## Paper 2 (Calculator)

### Higher Tier

#### Churchill Paper 2C – Marking Guide

Method marks (M) are awarded for a correct method which could lead to a correct answer

Accuracy marks (A) are awarded for a correct answer, having used a correct method, although this can be implied

(B) marks are awarded independent of method

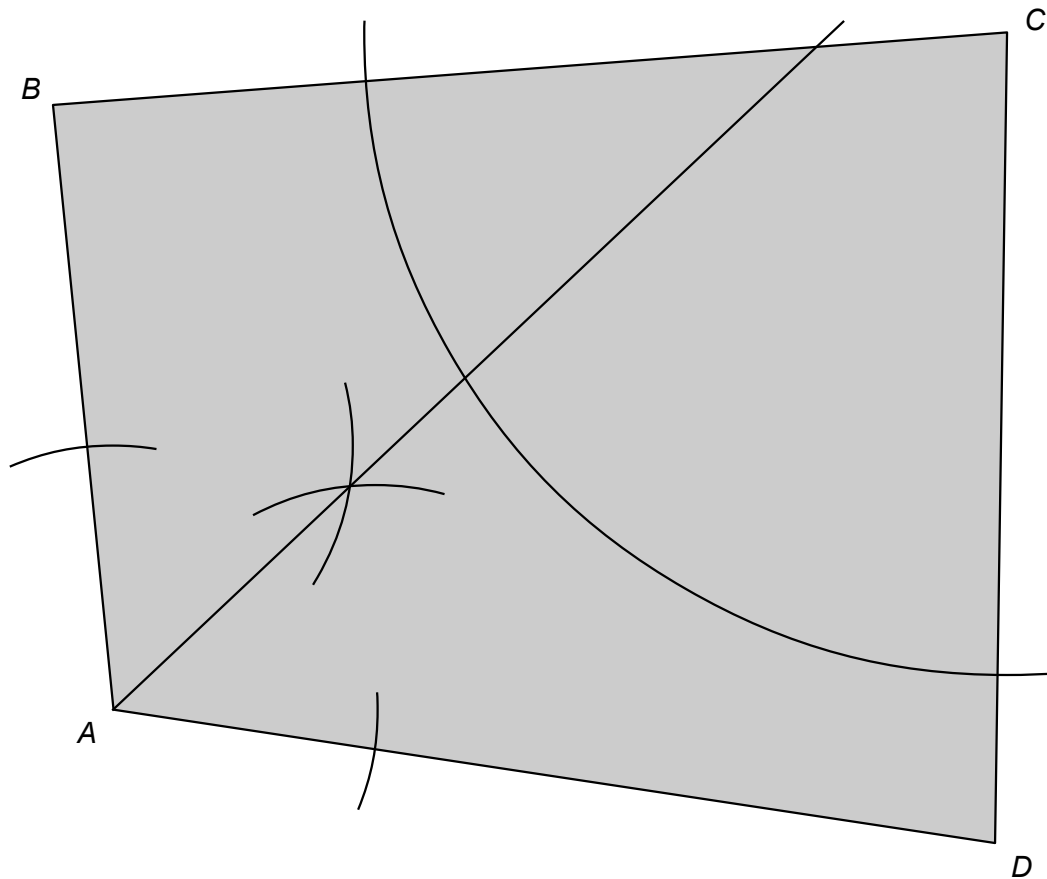


Written by Shaun Armstrong

Only to be copied for use in a single school or college having purchased a licence



6



Arc of circle centre C, radius 8.5 cm	B1	
Correct method of construction of bisector of angle BAC	M1	
On the drawing, distance $\approx 9.3$ cm	M1	
The tree is 465 m from D [ Accept 440 to 490 ]	A1	Total 4

7 (a)  $1 \text{ m}^2 = 100^2 \text{ cm}^2 = 10000 \text{ cm}^2$   
 $0.4 \text{ m}^2 = 0.4 \times 10000 = 4000 \text{ cm}^2$

40 cm<sup>2</sup>    4000 cm<sup>2</sup>    40 000 cm<sup>2</sup>    400 000 cm<sup>2</sup>    B1

(b) 5 miles =  $5 \times 5289 \text{ ft} = 26445 \text{ ft}$   
 $= 12 \times 26445 \text{ in} = 317340 \text{ in}$     M1  
 $= 2.54 \times 317340 \text{ cm} = 806043.6 \text{ cm}$   
 $= 8060.436 \text{ m}$   
 $= 8.060436 \text{ km}$     M1

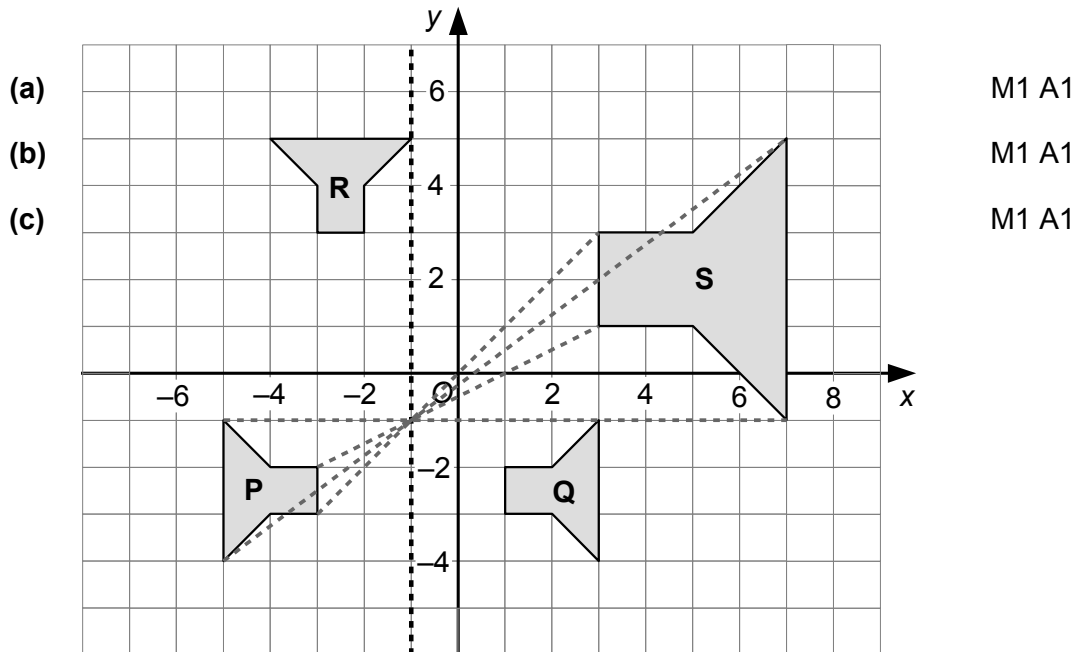
Error =  $8.060436 - 8 \text{ km} = 0.060436 \text{ km}$

% error =  $\frac{0.060436}{8.060436} \times 100\%$   
 $= 0.7497\% = 0.750\% \text{ (3sf)}$     A1    Total 4

- 8 (a)  $4m - 2 < 5$   
 $4m < 7$  M1  
 $m < \frac{7}{4}$  [ or  $m < 1.75$  ] A1
- (b)  $-12 + 7 \leq 4n \leq 5 + 7$  M1  
 $-5 \leq 4n \leq 12$   
 $-\frac{5}{4} \leq n \leq 3$  M1  
 $\{-1, 0, 1, 2, 3\}$  A1 Total 5

- 9 (a) Lily paid £12 to play 12 games  
£6 profit so she got  $6 + 12 = £18$  in winnings  
[Lily won  $18 \div 3 = 6$  times]  
Mila paid £25  
£4 loss so she got  $25 - 4 = £21$  in winnings  
[Mila won  $21 \div 3 = 7$  times]  
Mila won more games A1
- (b) Total games =  $12 + 25 = 37$   
Total winnings =  $18 + 21 = £39$   
No. of games won =  $39 \div 3 = 13$  M1  
Probability of winning =  $\frac{13}{37}$  A1
- (c) Owner received £200 for 200 games played  
Owner paid out  $200 - 32 = £168$   
No. of games won =  $168 \div 3 = 56$  M1  
Probability of winning =  $\frac{56}{200}$   
 $= \frac{7}{25}$  A1
- (d) e.g. The second estimate is likely to be more accurate as it is based on a larger number of games B1 Total 7

10

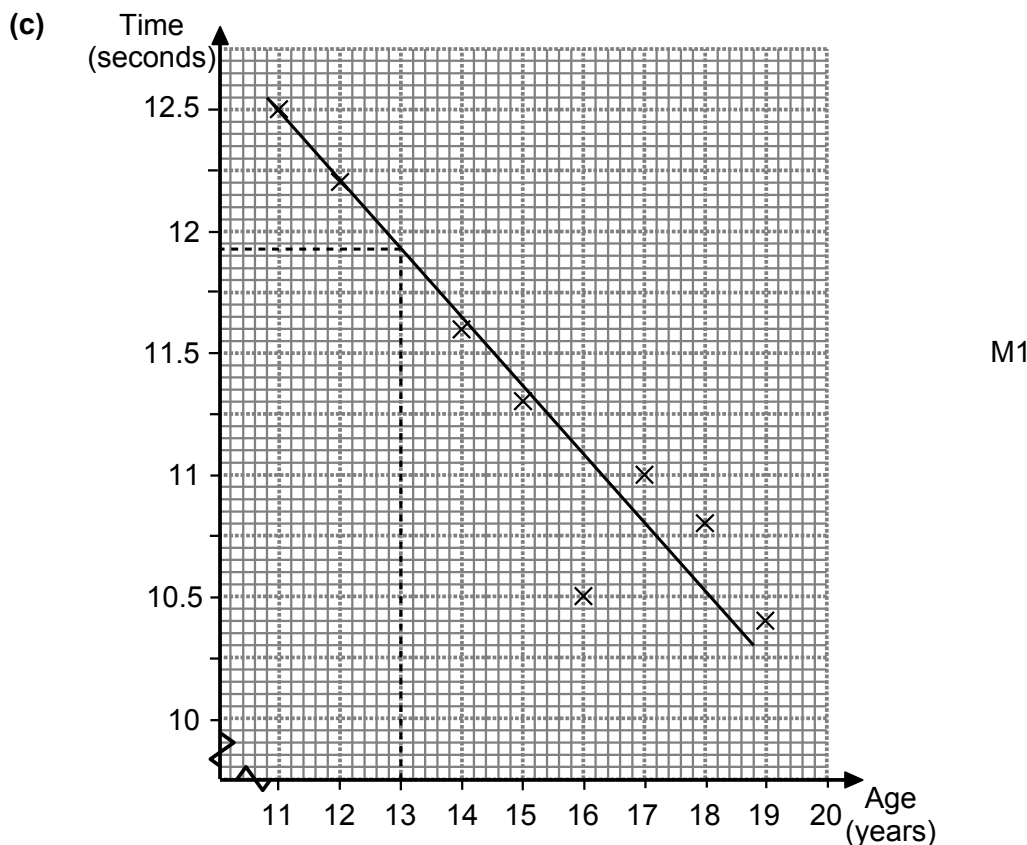


Total 6

11	$  \begin{aligned}  (\sqrt{6} + \sqrt{8})^2 &= (\sqrt{6} + \sqrt{8})(\sqrt{6} + \sqrt{8}) \\  &= 6 + \sqrt{6}\sqrt{8} + \sqrt{6}\sqrt{8} + 8 \\  &= 14 + \sqrt{48} + \sqrt{48} \\  &= 14 + 2\sqrt{48} \\  &= 14 + 2\sqrt{16 \times 3} \\  &= 14 + 2 \times 4\sqrt{3} \\  &= 14 + 8\sqrt{3}  \end{aligned}  $	M1	
		M1	
		A1	Total 3

12	e.g. Let first odd number be $2n + 1$ where $n$ is an integer Next 2 odd numbers are $2n + 3$ and $2n + 5$ Sum $= 2n + 1 + 2n + 3 + 2n + 5$ $= 6n + 9$ $= 3(2n + 3)$ $2n + 3$ is an integer so $3(2n + 3)$ will be a multiple of 3	M1	
		M1	
		A1	Total 3

13	(a) e.g. Because that point is an outlier – it does not fit with the trend of the rest of the data	B1	
	(b) e.g. No, because the points plotted are the best for each age – it only takes one exceptional athlete to produce an outlier so it could be correct	B1	



$\approx 11.9$ seconds (from line of best fit)	A1	
--	----	--

*[Line can consider or ignore the outlier]*

(d)	e.g. Because age 30 is outside the range of the data – it requires extrapolation and we don't know if the trend continues	B1	Total 5
-----	---	----	---------

- 14 Angle  $VWX = \text{exterior angle} = 360 \div 8 = 45^\circ$   
 Angle  $UVW = \text{interior angle} = 180 - 45 = 135^\circ$   
 By symmetry, angle  $RVW = 135 \div 2 = 67.5^\circ$   
 Angles on a straight line total  $180^\circ$  so angle  $WVX = 180 - 67.5 = 112.5^\circ$   
 Angles in a triangle total  $180^\circ$  so angle  $VXW = 180 - (45 + 112.5) = 22.5^\circ$

21.5°      22.5°      24°      25°      B1      Total 1

---

- 15  $81 = 3^4$ ,  $27 = 3^3$ ,  $9 = 3^2$  so  $(3^4)^{32} \times (3^3)^{40} = (3^2)^x$   
 $3^{128} \times 3^{120} = 3^{2x}$   
 $128 + 120 = 2x$   
 $x = 248 \div 2 = 124$

72      124      248      372      B1      Total 1

---

- 16 Volume =  $x \times (x - 2) \times 3$   
 $= 3x(x - 2)$

So  $3x(x - 2) = 72$       M1  
 $3x^2 - 6x - 72 = 0$   
 $x^2 - 2x - 24 = 0$   
 $(x + 4)(x - 6) = 0$       M1  
 $x = -4$  or  $6$

$x$  is a length so can't be negative, hence  $x = 6$       A1      Total 3

---

- 17 Volume of cylinder =  $\pi r^2 h$   
 Volume of coin =  $\pi \times (1.2)^2 \times 0.2 = 0.9047... \text{ cm}^3$       M1  
 Mass = volume  $\times$  density  
 Mass of coin =  $0.9047... \times 10.5 = 9.500... \text{ g}$       M1  
 $= 0.009500... \text{ kg}$   
 Number of atoms =  $0.009500... \div 1.79 \times 10^{-25}$       M1  
 $= 5.31 \times 10^{22}$  (3sf)      A1

Total 4

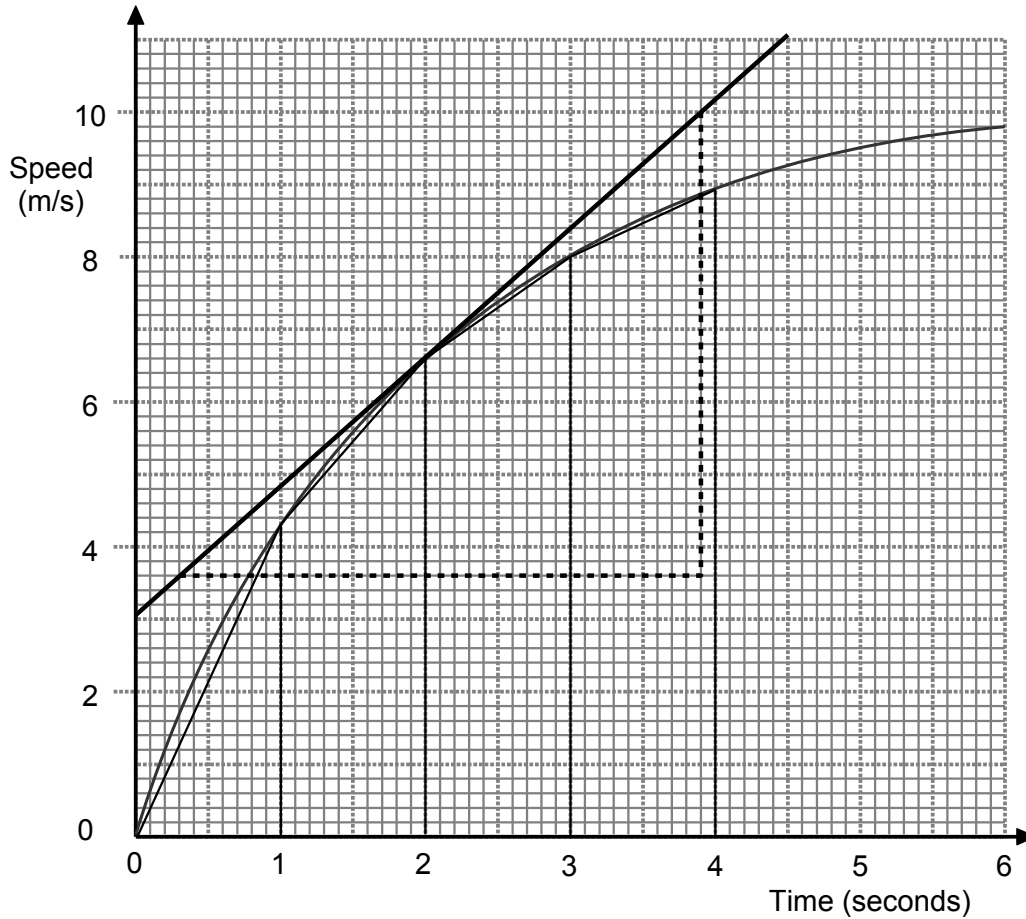
---

- 18 (a)  $= (x + 2)^2 - 2^2 + 7$       M1  
 $= (x + 2)^2 - 4 + 7$   
 $= (x + 2)^2 + 3$       A1

(b)  $(-2, 3)$       B1      Total 3

---

19 (a)



Acceleration = gradient of tangent M1  

$$\approx \frac{10 - 3.6}{3.9 - 0.3}$$
 M1  

$$= 1.777\dots$$
  
 Acceleration  $\approx 1.8 \text{ ms}^{-2}$  A1

(b) Distance = area under graph M2  

$$\approx \frac{1}{2} \times 1 \times 4.3 + \frac{1}{2} \times 1 \times (4.3 + 6.6)$$
  

$$+ \frac{1}{2} \times 1 \times (6.6 + 8) + \frac{1}{2} \times 1 \times (8 + 8.9)$$
  

$$= \frac{1}{2} \times (4.3 + 10.9 + 14.6 + 16.9) = \frac{1}{2} \times 46.7 = 23.35$$
  
 Distance  $\approx 23 \text{ m}$  A1

(c) Underestimate as the graph is above the top of the triangle and trapeziums used B1 Total 7

<b>20</b>	<b>(a)</b>	$f(-2) = [5 \times (-2)] - 2 = -12$ $ff(-2) = f(-12) = [5 \times (-12)] - 2 = -62$					
		-62	-42	3	18	B1	
	<b>(b)</b>	Let $y = f(x)$ so $y = 5x - 2$ For inverse, swap $x$ and $y$ :	$x = 5y - 2$ $x + 2 = 5y$ $\frac{x + 2}{5} = y$			M1	
		Hence, $f^{-1}(x) = \frac{x + 2}{5}$				A1	Total 3

<b>21</b>	For up to 3 years the first account is better				B1	
	First account	4 years: $(1.03)^4 \times 4000 = 4502$ 5 years: $(1.03)^5 \times 4000 = 4637$ (4637.10) 6 years: $(1.03)^6 \times 4000 = 4776$			M1	
	Second account	4 years: $1.02 \times 1.025 \times 1.03 \times 1.035 \times 4000 = 4458$ 5 years: $1.04 \times 4458.22 = 4637$ (4636.55) 6 years: $1.045 \times 4636.55 = 4845$			M1	
	e.g. If you are likely to withdraw the money within 5 years you should choose the first account to gain the most interest. If you are more likely to leave the money in the account for longer then the second account pays more (with the difference increasing more quickly the longer you leave it in).				M1	
					A1	Total 5

<b>22</b>	Area of rectangle = $12 \times 10 = 120 \text{ cm}^2$ Area of quadrilateral = area of rectangle – areas of 4 white triangles Length from $A$ to top left corner = $12 - 4 = 8 \text{ cm}$ Length from $D$ to top left corner = $(10 - x) \text{ cm}$ Areas of triangles: $\frac{1}{2} \times 4 \times 5 = 10$ , $\frac{1}{2} \times 5 \times 6 = 15$ , $\frac{1}{2} \times 6 \times x = 3x$ , $\frac{1}{2} \times 8 \times (10 - x) = 40 - 4x$				M1	
	Area of quadrilateral = $120 - 10 - 15 - 3x - (40 - 4x)$ $= 95 - 3x - 40 + 4x$ $= 55 + x$				M1	
	As $0 \leq x \leq 10$ , maximum area = $55 + 10 = 65 \text{ cm}^2$				A1	
	[Alternatively can consider maximum area of triangle $ACD$ with $AC$ as base. Greatest perpendicular height when $D$ is at top left etc.]					Total 4

**TOTAL FOR PAPER: 80 MARKS**